

$$j := \sqrt{-1} \quad \text{MVA} := \text{MW} \quad \text{pu} := 1 \quad \text{Tpu} := 1$$

3.62 A three-phase transformer is rated 1 GW, 13.8kV Δ /345 kV Y with $Z_{\text{eq}} = j 0.10$ per unit. The transformer high-voltage winding has plus or minus 10% taps. The system base quantities are:

$$S_{\text{base_sys}} := 500 \cdot \text{MVA}$$

$$V_{\text{base_XLL}} := 13.8 \cdot \text{kV}$$

$$V_{\text{base_HLL}} := 345 \cdot \text{kV}$$

Determine the per-unit equivalent circuit for the following tap settings:

- Rated tap and
- + 10% tap (providing 10% voltage increase for the high-voltage winding.)

$$Z_{\text{base_sysH}} := \frac{V_{\text{base_HLL}}^2}{S_{\text{base_sys}}} \quad Z_{\text{base_sysH}} = 238.05 \, \Omega$$

$$Z_{\text{eq}} := j \cdot 0.10 \cdot \text{Tpu}$$

$$S_{\text{base_T}} := 1000 \cdot \text{MVA}$$

$$Z_{\text{base_T}} := \frac{V_{\text{base_HLL}}^2}{S_{\text{base_T}}} \quad Z_{\text{base_T}} = 119.025 \, \Omega$$

a.

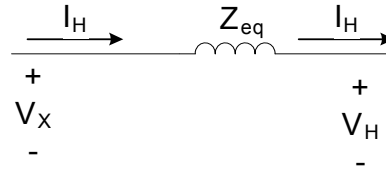
$$a_t := \frac{13.8 \cdot \text{kV}}{345 \cdot \text{kV}} \quad a_t = 0.040$$

$$b := \frac{V_{\text{base_XLL}}}{V_{\text{base_HLL}}} \quad b = 0.040$$

$$c := \frac{a_t}{b} \quad c = 1$$

$$Z_{pu_sys} := \frac{Z_{eq} \cdot Z_{base_T}}{Z_{base_sysH}}$$

$$Z_{pu_sys} = 0.05j \cdot pu$$



b.

$$a_{tp10} := \frac{13.8 \cdot kV}{1.1 \cdot 345 \cdot kV}$$

$$a_{tp10} = 0.036$$

$$c := \frac{a_{tp10}}{b}$$

$$c = 0.909$$

$$Y_{eq} := \frac{1}{Z_{pu_sys}}$$

$$Y_{eq} = -20j \cdot pu$$

$$\frac{1}{Y_{eq}} = 0.05j \cdot pu$$

$$c \cdot Y_{eq} = -18.182j \cdot pu$$

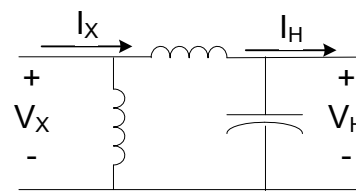
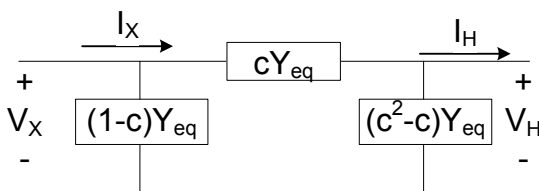
$$\frac{1}{c \cdot Y_{eq}} = 0.055j \cdot pu \quad \text{inductor}$$

$$(1 - c)Y_{eq} = -1.818j \cdot pu$$

$$\frac{1}{(1 - c) \cdot Y_{eq}} = 0.55j \cdot pu \quad \text{inductor}$$

$$(c^2 - c)Y_{eq} = 1.653j \cdot pu$$

$$\frac{1}{(c^2 - c) \cdot Y_{eq}} = -0.605j \cdot pu \quad \text{capacitor}$$



For fun determine the admittance looking in the low side with the high side open circuited.

$$Y_{\text{series}} := \frac{c \cdot Y_{\text{eq}} \cdot (c^2 - c) \cdot Y_{\text{eq}}}{c \cdot Y_{\text{eq}} + (c^2 - c) \cdot Y_{\text{eq}}} \quad Y_{\text{series}} = 1.818j \cdot \text{pu}$$

$$(1 - c) \cdot Y_{\text{eq}} = -1.818j \cdot \text{pu}$$

$$Y_{\text{parallel}} := Y_{\text{series}} + (1 - c) \cdot Y_{\text{eq}} \quad Y_{\text{parallel}} = 0 \cdot \text{pu}$$

- 4.18 A 230-kV, 60 Hz, three-phase completely transposed overhead line has one ACSR 954-kcmil conductor per phase and flat horizontal phase spacing, with 8 m between adjacent conductors.

Determine the inductance in H/m and the inductive reactance in Ω/km .

Looking at Table A.4: Cardinal has 954-kcmil.

$$r' := 0.0403 \cdot \text{ft}$$

$$r' = 1.228 \cdot \text{cm}$$

$$D_{12} := 8 \cdot \text{m}$$

$$D_{13} := 16 \cdot \text{m}$$

$$D_{23} := 8 \cdot \text{m}$$

$$D_s := \sqrt[3]{D_{12} \cdot D_{13} \cdot D_{23}}$$

$$D_s = 10.079 \cdot \text{m}$$

$$L_a := 2 \cdot 10^{-7} \cdot \frac{\text{H}}{\text{m}} \cdot \ln\left(\frac{D_s}{r'}\right)$$

$$L_a = 1.342 \times 10^{-6} \cdot \frac{\text{H}}{\text{m}}$$

$$X_a := 2 \cdot \pi \cdot 60 \cdot \text{Hz} \cdot L_a$$

$$X_a = 0.506 \cdot \frac{\Omega}{\text{km}}$$

4.19 Rework Problem 4.18 if the phase spacing between adjacent conductors is:

- increased by 10% to 8.8 m,
- decreased by 10% to 7.2 m.

Compare the results with those of Problem 4.18

a.

$$D_{12i} := 8.8 \cdot \text{m}$$

$$D_{13i} := 17.6 \cdot \text{m}$$

$$D_{23i} := 8.8 \cdot \text{m}$$

$$D_{si} := \sqrt[3]{D_{12i} \cdot D_{13i} \cdot D_{23i}}$$

$$D_{si} = 11.087 \cdot \text{m}$$

$$L_{ai} := 2 \cdot 10^{-7} \cdot \frac{\text{H}}{\text{m}} \cdot \ln\left(\frac{D_{si}}{r'}\right)$$

$$L_{ai} = 1.361 \times 10^{-6} \cdot \frac{\text{H}}{\text{m}}$$

$$\frac{L_{ai} - L_a}{L_a} = 1.42\%$$

$$X_{ai} := 2 \cdot \pi \cdot 60 \cdot \text{Hz} \cdot L_{ai}$$

$$X_{ai} = 0.513 \cdot \frac{\Omega}{\text{km}}$$

$$\frac{X_{ai} - X_a}{X_a} = 1.42\%$$

b.

$$D_{12d} := 7.2 \cdot \text{m}$$

$$D_{13d} := 14.4 \cdot \text{m}$$

$$D_{23d} := 7.2 \cdot \text{m}$$

$$D_{sd} := \sqrt[3]{D_{12d} \cdot D_{13d} \cdot D_{23d}}$$

$$D_{sd} = 9.071 \cdot \text{m}$$

$$L_{ad} := 2 \cdot 10^{-7} \cdot \frac{\text{H}}{\text{m}} \cdot \ln\left(\frac{D_{sd}}{r'}\right)$$

$$L_{ad} = 1.321 \times 10^{-6} \cdot \frac{\text{H}}{\text{m}}$$

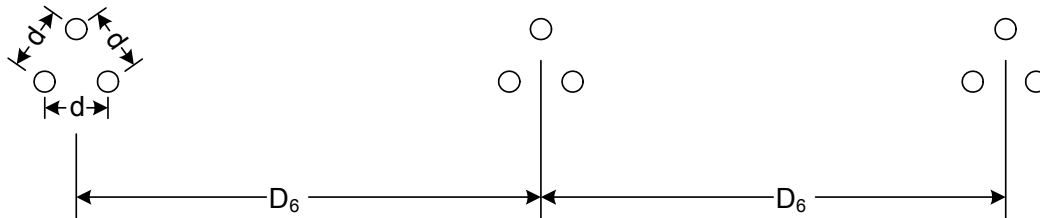
$$\frac{L_{ad} - L_a}{L_a} = -1.57\%$$

$$X_{ad} := 2 \cdot \pi \cdot 60 \cdot \text{Hz} \cdot L_{ad}$$

$$X_{ad} = 0.498 \cdot \frac{\Omega}{\text{km}}$$

$$\frac{X_{ad} - X_a}{X_a} = -1.57\%$$

- 4.20** Calculate the inductive reactance in Ω/km of a bundled, 60 Hz, three-phase completely transposed overhead line having three ACSR 1113-kcmil conductors per bundle, with 0.5m between conductors in the bundle. The horizontal spacing between bundle centers are 10, 10, and 20 m



$$d := 0.5 \cdot \text{m}$$

$$D_6 := 10 \cdot \text{m}$$

Looking at Table A.4: Finch has 1113-kcmil.

Calculate the GMR

$$r'_6 := 0.0435 \cdot \text{ft}$$

$$r'_6 = 1.326 \cdot \text{cm}$$

$$D_{SL} := \sqrt[3]{r'_6 \cdot d^2}$$

$$D_{SL} = 0.149 \text{ m}$$

Calculate the GMD

$$D_{126} := D_6$$

$$D_{136} := 2 \cdot D_6$$

$$D_{236} := D_6$$

$$D_{s6} := \sqrt[3]{D_{126} \cdot D_{236} \cdot D_{136}}$$

$$D_{s6} = 12.599 \text{ m}$$

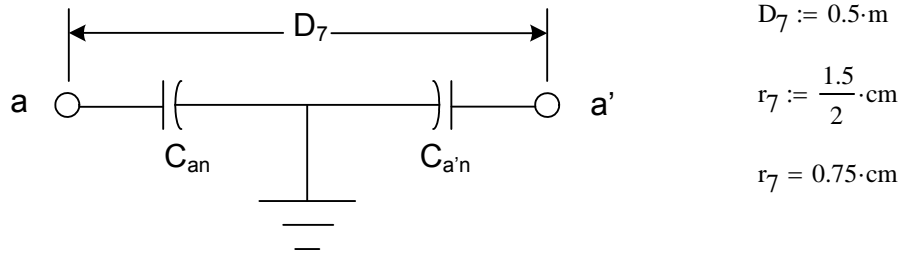
Calculate the inductive reactance

$$X_{L6} := 2 \cdot \pi \cdot 60 \cdot \text{Hz} \cdot 2 \cdot 10^{-7} \cdot \frac{\text{H}}{\text{m}} \cdot \ln \left(\frac{D_{s6}}{D_{SL}} \right)$$

$$X_{L6} = 0.335 \cdot \frac{\Omega}{\text{km}}$$

4.32 Calculate the capacitance-to-neutral in F/m and admittance-to-neutral in S/km for the single-phase line in Problem 4.8. Neglect the effect of the earth plane.

(4.8 A 60 Hz single-phase, two-wire overhead line has solid cylindrical copper conductors with 1.5 cm diameter. The conductors are arranged in a horizontal configuration with 0.5 m spacing.)



$$\epsilon_0 = 8.854 \times 10^{-12} \cdot \frac{\text{F}}{\text{m}}$$

$$C_{\text{an}} := \frac{2 \cdot \pi \cdot \epsilon_0}{\ln\left(\frac{D_7}{r_7}\right)}$$

$$C_{\text{an}} = 13.247 \times 10^{-12} \cdot \frac{\text{F}}{\text{m}}$$

$$Y_{\text{an}} := j \cdot 2 \cdot \pi \cdot 60 \cdot \text{Hz} \cdot C_{\text{an}}$$

$$Y_{\text{an}} = 4.994j \times 10^{-6} \cdot \frac{\text{S}}{\text{km}}$$

OR

$$Z_{\text{an}} := \frac{1}{j \cdot 2 \cdot \pi \cdot 60 \cdot \text{Hz} \cdot C_{\text{an}}}$$

$$Z_{\text{an}} = -2.002j \times 10^8 \cdot \Omega \cdot \text{m}$$

$$Y_{\text{an}} := \frac{1}{Z_{\text{an}}}$$

$$Y_{\text{an}} = 4.994j \times 10^{-6} \cdot \frac{\text{S}}{\text{km}}$$